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## An MLP- $P_1$ model for the scattering coefficient estimation from total incident radiation measurements

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In this work we present an artificial neural network (ANN) model for the scattering coefficient estimation from total incident radiation measurements in a participating media. The inverse radiative heat transfer problem is set as a regression problem that has the total incident radiation measurements as dependent variables. The heat transfer is assumed to be modeled in an one dimensional domain D = [a, b], in a medium with known absorption coefficient  $\kappa$  and heat radiation source. The scattering coefficient  $\sigma$  is the independent variable.

The regression model is built as a Multi-layer Perceptron (MLP) artificial neural network model [2]. Following a supervised training strategy, the MLP is calibrated from known  $n_{\text{train}}$  samples selected for this end. Any given *j*-th sample is a pair  $X_k = (\{\Phi_i^{(k)}\}_{i=0}^{n_v-1}, \sigma_k)$ , where  $\Phi_i^{(k)} = \Phi^{(k)}(x_i)$  is the total incident radiation measured at the vertex  $x_i \in D$ , and  $n_v$  is the fixed number of vertices (measurement's locations).

Each calibration sample  $X_K$  is built by choosing the scattering coefficient  $\sigma_k$  and, then, computing  $\Phi^{(k)}$  by solving the direct radiative heat transfer problem. The  $P_1$  approximation [1,3,5] is used to compute the total incident radiation. Once the calibration is computed, the MLP can be calibrated. The MLP has been computed using the machine learning Python package scikit-learn [6]. The  $SP_1$  approximation has been computed using the finite element Python package FEniCS [4].

The validation of the MLP model has been performed by applying  $n_{\text{valid}}$  validation samples. Here, each validation sample  $j = 0, 1, \ldots, n_{valid}$  has been built by randomly fixing the  $\sigma_k$  value and, then, the related  $\Phi^{(k)}$  is computed from the  $P_1$  approximation of the direct radiative heat transfer problem.

As a test case, lets considered D = [0, 1], a homogeneous medium with the absorption coefficient  $\kappa = 1$ , and temperature T(x) = 1000 + 800x,  $x \in D$ . For this case, we have built a calibration set with  $n_{\text{train}} = 11$ ,  $\sigma_k = 0.1k$ ,  $k = 0, 1, \ldots, n_{\text{train}} - 1$ , and  $\Phi_i^{(k)} = \Phi^{(k)}(x_i)$ , where  $x_i = 0.25i$ ,  $i = 0, 1, \ldots, n_v - 1$ ,  $n_v = 5$ . Here, a MLP with one hidden layer (5 hidden neurons) has been sufficient to reach a calibration curve with  $R^2 = 0.99$ . The MLP has been then validated using a validation set with 25 random samples with  $0 \le \sigma_j \le 1$ . Again, a very good validation curve has been found with  $R^2 = 0.99$ . The results indicates the potentiality of the proposed methodology as a tool to estimate the scattering parameter of radiative objects.

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